

Setting up Truth Trees to check for semantic properties other than consistency:

Check if **P** is a Tautology:

1. $\sim P$ SM

If and only if the tree for $\{\sim P\}$ closes, **P** is a tautology.

Check if **P** is a Contradiction:

1. **P** SM

If and only if the tree for $\{P\}$ closes, **P** is a contradiction.

Check if **P** is Contingent:

If and only if neither the tree for $\{P\}$ nor for $\{\sim P\}$ closes, **P** is contingent.

Check for Equivalence of **P** and **Q**:

1. $\sim(P \equiv Q)$ SM

If and only if the tree for $\{\sim(P \equiv Q)\}$ closes, **P** and **Q** are truth-functionally equivalent.

Check whether $\{P, Q, R\}$ Entails **S**:

1. **P** SM
2. **Q** SM
3. **R** SM
4. $\sim S$ SM

If and only if the tree for $\{P, Q, R, \sim S\}$ closes, then $\{P, Q, R\}$ entails **S**.

Check whether the argument below is Valid:

P1: **P**

P2: **Q**

P3: **R**

C: **S**

1. **P** SM
2. **Q** SM
3. **R** SM
4. $\sim S$ SM

If and only if the tree for $\{P, Q, R, \sim S\}$ closes, the argument above is valid